## 2. Theory

According to Bohr's theory, atoms can only remain stable in some specific states (i.e. steady-states). Each of which corresponds to a certain amount of energy, and the steady-state energy is discrete. Atoms can only absorb or release the energy amount that is equivalent to the energy difference between two discrete states. To excite an atom from the ground state to the first excitation state, the impact energy must not be less than the energy difference between the two states. Franck-Hertz experiment implements the energy exchange for state transitions through the collisions of atoms with electrons of certain energy. The electron energy is obtained by applying an accelerating electric field. The process can be represented by using the equation below:

$$\frac{1}{2}m_e v^2 \ge eV_1 = E_1 - E_0$$

where e,  $m_e$  and v are the charge, mass and speed (before collision) of an electron, respectively.  $E_1$  and  $E_0$  are the energy of an atom at the  $1^{st}$  excitation state and the ground state, respectively.  $V_1$  is the minimum voltage of the accelerating field required to excite the atom from the ground state to the  $1^{st}$  excitation state, which is called as the first excitation potential of the atom.  $eV_1$  is therefore called as the  $1^{st}$  excitation potential energy.

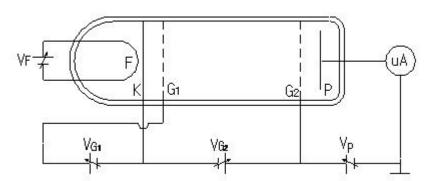


Figure 1 Schematic of Franck-Hertz experiment

The principle of the Franck-Hertz experiment is shown in Figure 1. In an Argon-filled Franck-Hertz tube (F-H tube), electrons are emitted from hot cathode K. A relatively low voltage  $V_{\rm Gl}$  is applied between cathode K and grid  $G_1$  to control the electron flow entering the collision region. An adjustable accelerating voltage,  $V_{\rm G2}$ , is applied between grid  $G_2$  and cathode K to accelerate electrons to desired energy. A braking voltage  $V_{\rm p}$  is applied between anode P and grid  $G_2$ . The electric potential distribution in the F-H tube is shown in Figure 2. When electrons pass through grid  $G_2$ , they can arrive at anode P to form current  $I_{\rm p}$  if their energy is higher than  $eV_{\rm p}$ .

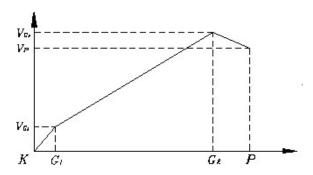


Figure 2 Schematic of potential distribution in the F-H tube

At the beginning, accelerating voltage  $V_{\rm G2}$  is relatively low, the energy of electrons arriving at grid  $G_2$  is less than  $eV_{\rm p}$ , so the electrons cannot reach anode P to form a current. By increasing  $V_{\rm G2}$ , the electron energy increases accordingly, so does current  $I_{\rm p}$ . As a result, the electrons with energy larger than the 1<sup>st</sup> excitation potential energy pass energy amount  $eV_1$  to the argon atoms by inelastic collisions, and subsequently their residual energy is less than  $eV_{\rm p}$ , resulting in a decrease in anode current  $I_{\rm p}$ .

By continuously increasing  $V_{\rm G2}$ , anode current  $I_{\rm p}$  increases again. The electrons regain energy over the 1<sup>st</sup> excitation potential energy and then lose energy amount  $eV_1$  to argon atoms due to the second inelastic collision, leading to the second decline in anode current. By continuously increasing  $V_{\rm G2}$ , multiple inelastic collisions occur between electrons and Argon atoms. There will be multiple rise/fall cycles on the  $I_P \sim V_{G_2}$  curve, as shown in Figure 3.

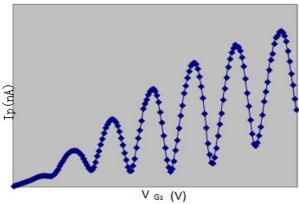


Figure 3 Relationship curve of anode current  $I_p$  with accelerating voltage  $V_{G_2}$ 

For argon atoms, the voltage difference between adjacent peaks or valleys as shown in Figure 3 is the 1<sup>st</sup> excitation potential of the argon atom, thus proving the discontinuity of argon atomic energy states.

The absorbed energy of the argon atom will be released through electron transition to lower state, and therefore a strong emission spectral line can be found that is corresponding to an energy of  $eV_1$ . According to published literatures, the measured argon atom resonance line is 106.7 nm (or 11.62 eV). Using the acquired 1<sup>st</sup> excitation potential, Planck's constant h can be calculated based on the formula:  $h = eV_1\lambda/c$ , where  $e=1.602\times10^{-19}$  C,  $\lambda=106.7$  nm, and  $c=3\times10^8$  m/s.